

# Parsing Shade

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**ABSTRACT** - Spectral Mixture Analysis (SMA) is a standard way of analyzing spectral images in terms of fundamental components of the scene. It accounts for lighting variations by using a *Shade* endmember that mixes with the tangible spectral endmembers such as green vegetation to produce observed spectral radiances. In forests, *Shade* comprises shadowing and topographic shading ("hillshade"), unresolved shadows cast by the canopy ("treeshade"), and shading plus shadows cast by elements of the canopy ("leafshade"). We use a 1-m LiDAR DEM to model *treeshade* over a low-relief forested area, and SMA to calculate *Shade* for an ASTER image of the same area taken near the same time of year. The differences between *treeshade* and *Shade* give remote-sensing estimates of *leafshade* in a forest dominated by deciduous trees.

**Research goal** - analyze image shade in a forest in terms of its unresolved constituent parts: *treeshade* and *leafshade*  $\Lambda$ , and make an image of  $\Lambda$ .

## Spectral Mixture Analysis and an analytic framework

### Fundamental equations

Forward linear mixing model

$$L_i = \sum_j f_j E_{ij} + \delta_i; \quad m < n+1; \quad \sum_j f_j = 1$$

$L$  spectral radiance ( $Wm^{-2}\mu m^{-1}sr^{-1}$ ) in image channel  $i$   
 $E$   $L$  vector for spectral endmember  $j$  in image channel  $i$   
 $f$  fraction of endmember spectrum  $E$  needed to model  $L_i$  for a specific pixel  
 $\delta$  unmodeled residual for channel  $i$   
 $m$  number of spectral endmembers  
 $n$  number of spectral image channels

### Endmember spectra defined

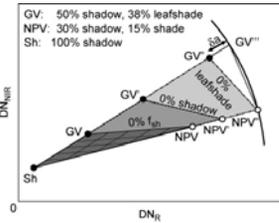
in ASTER image DN (VNIR channels 1-3: Green, Red, NIR)

Shade (Sh)	51	27	30
Green Vegetation (GV)	78	37	134
Non-photosynthetic vegetation (NPV)	173	146	110

### Shade endmember

$c_0 + c_1 f_{sh} = S + (1-S) \Lambda + (1-S)(1-\Lambda)(1-a)\chi(i)$   
 $f_{sh}$  Shade fraction (1 = *Shade* endmember; 0 = the GV-NPV mixing line)  
 $c_0, c_1$  calibration offset and gain factor. Image-defined endmembers may contain a fraction of shade, but  $f_{sh} = 0.0$  should correspond to zero shade. The *Shade* endmember itself is defined as 100% shade.  
 $S$  *treeshade* shadow fraction, integrated to the image scale. Shadows unresolved by the LiDAR are included as a component of leafshade.  
 $\chi$  integrated reflectance for the sunlit part of the canopy. For Lambertian surfaces,  $\chi = 1 - \cos(i)$ , where  $i$  is the solar incidence angle; for real canopies scattering is not diffuse. For uniform reflectance,  $\chi = 1$  (this example), independent of  $i$ .  
 $a$  relative albedo, the change in  $f_{sh}$  caused by absorption of light by the surface (e.g., a leaf) relative to the albedo of tangible endmember. Albedo is a property of composition, not structure.  
 $\Lambda$  leafshade shadow fraction, defined shadows cast by unresolved leaves and branches, integrated to the image scale. Leafshade is a property of structure, not composition.

**Calibration and solution for  $\Lambda$**  - We measured total shade  $f_{sh}$  from SMA of 15-m ASTER data and *treeshade*  $S$  using high-resolution 1-m LiDAR. Assuming  $a$  &  $\Lambda$  are constant for similar forest stands, we solved the shade endmember equation for  $c_1$  (calibration) and  $f_{sh}$ , using two or more similar stands with different  $f_{sh}$  and  $S$ .  $c_0$  was -0.66; Gain  $c_1$  was 2.58. Knowing  $c_0, c_1, f_{sh}$ , and  $S$ , we can solve for  $\Lambda$  for all pixels.



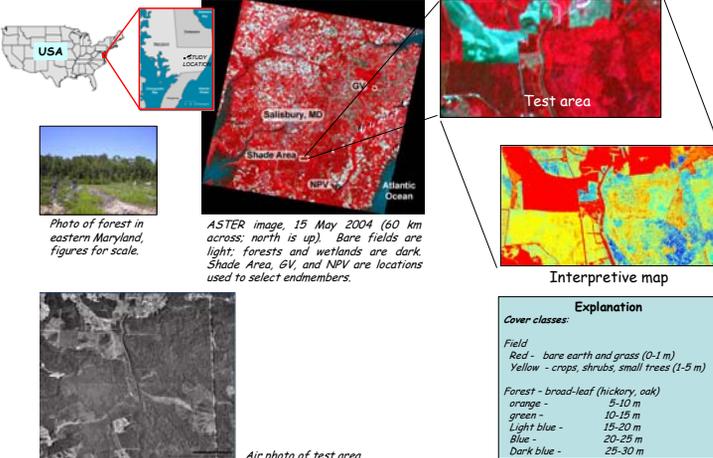
Schematic mixing diagram for the ASTER channel 3 (NIR) vs. channel 2 (R) plane. Arc is locus of a vector rotated about Sh.

The mixing plane for *Sh*, *GV* and *NPV* is shaded dark gray and shows isolines for  $f_{sh}=0$  (no shade), 0.2, 0.4, 0.6, and 0.8;  $f_{sh}=1$  (full shade) plots at *Sh*. Isolines for *NPV* (but not *GV*) are also shown. Shaded *GV* plots along the *GV*-*Sh* line; mixtures of *GV* and *NPV* plot along the  $f_{sh}=0$  line. Mixtures with less shade than in endmembers *GV* and *NPV* ( $f_{sh}<0$ ) plot beyond the  $f_{sh}=0$  isoline.

After calibration  $f_{sh}$ , *GV* and *NPV* endmembers with no shadows plot on their respective mixing lines with *Sh* (*GV* & *NPV*). Leafshade is unchanged. Mixing now occurs in the (*Sh*, *GV*, *NPV*) triangle shaded intermediate gray, and the isolines for  $f_{sh}$  may be discordant with the ones in the (*Sh*, *GV*, *NPV*) triangle. All image data will now plot within the new triangle (no negative *Sh* fractions).

Extrapolation to *GV* and *NPV* gives virtual endmember positions assuming leafshade is also zero, as might occur looking down-sun. *GV* and *NPV* may have different albedos such that vector *Sh*-*GV* is shorter than vector *Sh*-*NPV*; the difference is a measure of the difference in albedo  $a$ .  $GV''$  is the position that *GV* at zero phase angle would have if the albedoes were the same.

## Test site -



**Explanation**

Cover classes:

Field  
 Red - bare earth and grass (0-1 m)  
 Yellow - crops, shrubs, small trees (1-5 m)

Forest - broad-leaf (hickory, oak)  
 orange - 5-10 m  
 green - 10-15 m  
 Light blue - 15-20 m  
 Blue - 20-25 m  
 Dark blue - 25-30 m

## LiDAR images



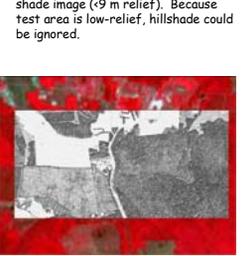
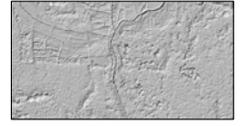
First-arrival LiDAR shade image, at full 1-m resolution and complemented so that areas of high shade are dark, as would be seen in an air photo (2.6 km across). North is up. Image shows  $S(1-S)\chi(1-a)\Lambda$ .

**Explanation**

Numbers indicate cover classes shown in interpretive map and identified by color:

Field  
 1 - red: bare earth and grass  
 2 - yellow: crops, shrubs, small trees

Forest  
 3 - orange: 5-10 m  
 4 - green: 10-15 m  
 5 - light blue: 15-20 m  
 6 - blue: 20-25 m  
 7 - dark blue: 25-30 m

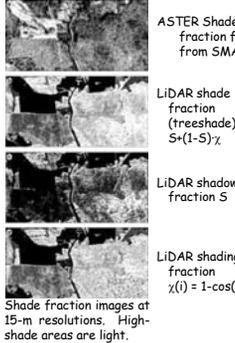


We extracted LiDAR images of the test area from data acquired by the State of Maryland's Department of Natural Resources between June and July of 2003. First-return point-cloud postings were 1 m, and vertical resolution was 14.3 cm.

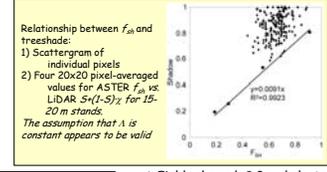
1st-arrival 1-m LiDAR shade image embedded in 15-m ASTER image. For calculation of  $\Lambda$ , LiDAR images were smoothed with 15 x 15 low-pass box filters, and resampled to 15-m resolution.

$S$  &  $S\chi$  images were calculated from the 1st-arrival data using ArcInfo and ERDAS Imagine, respectively.

## Results



ASTER Shade fraction  $f_{sh}$  from SMA  
 LiDAR shade fraction (treeshade)  $S(1-S)\chi$   
 LiDAR shadow fraction  $S$   
 LiDAR shading fraction  $\chi(i) = 1 - \cos(i)$

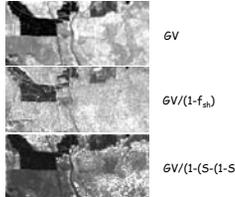


Relationship between  $f_{sh}$  and treeshade:  
 1) Scattergram of individual pixels  
 2) Four 20x20 pixel-averaged values for ASTER  $f_{sh}$  vs. LiDAR  $S(1-S)\chi$  for 15-20 m stands.  
 The assumption that  $\Lambda$  is constant appears to be valid

$\chi$  Fields showed  $S=0$  and plants were probably not resolved.  $f_{sh}$  was dominated by  $a$ .  
 $\chi$  Calibration gain  $c_1=2.58$   
 $\chi$  Assumption that  $\Lambda$  is constant for stands within a given age/size range is ~valid  
 $\chi$  Permits calculation of  $\Lambda$  for entire image  
 $\chi$   $\Lambda$  and  $S$  have similar variability.  $\Lambda=0.77$   
 $\chi$   $a=23\%$ : ASTER spectral library <http://speclib.lsa.nasa.gov>

## Discussion

### Normalization of $GV$



$\chi$   $S$  is highly variable and responds to structural stage  
 $\chi$   $(1-a)\Lambda$  appears to be less variable than  $S$ , and may prove useful in community mapping.  
 $\chi$  The approximated version of leafshade has higher variance because it retains a component of shadow and shading. It is easier to calculate.  
 $\chi$   $a$  and  $\Lambda$  are not separable by this approach.  
 $\chi$  In SMA, it is common to normalize "tangible" endmember fractions such as  $f_{GV}$  by  $(1-f_{sh})$ .  $f_{sh}$  includes effects due to  $a$  as well as  $\Lambda$ .  
 $\chi$  Normalizing by LiDAR shade images, independent of  $a$  and  $\Lambda$ , produces a different result that deserves field validation and further exploration.  
 $\chi$  Future work will take hillshade into account for rough forested terrain

## Conclusions

Remotely sensed spectral images integrate the effects of lighting up to the pixel scale. Blending contributions from topography, canopies, and leaves and branches. Hybrid analysis of spectral and LiDAR images can be used to separate contributions from shadows at the tree and stand scales and shading at sub-tree scales, and spectral mixture models can be calibrated so that spectral shade fractions ( $f_{sh}$ ) correspond to more direct measurements from LiDAR. For a deciduous forest in coastal Maryland, USA, viewed in late morning during early summer, leafshade was typically  $\sim 0.5 \pm 0.1$  vs. treeshade of  $\sim 0.92 \pm 0.08$ . Future analysis is necessary to account for topographic shading and shadowing, to incorporate a more accurate photometric function  $\chi$ , and to separate darkening due to albedo  $a$  on a pixel-by-pixel basis.

## Bibliography

- Adams, J. B., and Gillespie, A. R., 2006. *Remote Sensing of Landscapes with Spectral Images: A Physical Modeling Approach*. Cambridge University Press, Cambridge, UK, 362 pp.
- Adams, J. B., Smith, M. O., and Johnson, P. E., 1986. Spectral mixture modeling: a new analysis of rock and soil types at the Viking Lander I site. *Journal of Geophysical Research* 91, 8098-8112.
- Dymond, J., Shephard, J. D., and Qi, J., 2001. A simple physical model of vegetation canopy reflectance. *Remote Sensing of Environment* 75, 35-35.
- Gu, D., and Gillespie, A. R., 1998. Topographic normalization of Landsat TM images of forests based on subpixel sun-canopy sensor geometry. *Remote Sensing of Environment* 64, 166-175.
- Franklin, J., Davis, F. W., and Lefebvre, P., 1991. Thematic Mapper analysis of tree cover in semiarid woodlands using a model of canopy shadowing. *Remote Sensing of Environment* 36, 189-202.
- Hall, F. G., Knapp, D. E., and Huemmrich, K. F., 1997. Physically based classification and satellite mapping of biophysical characteristics in the southern boreal forest. *Journal of Geophysical Research* 102(D24), 29 567-29 580.
- Kaithi, R. J., and Thomas, S. S., 1976. The tasseled cap - a graphic description of the spectral temporal development of agricultural crops as seen by Landsat. *Proceedings, Machine Processing of Remotely Sensed Data*. Purdue Univ., IN, pp. 41-51.
- Li, X., Strahler, A. H., and Woodcock, C. E., 1995. A hybrid geometric optical radiative transfer approach for modeling albedo and directional reflectance of discontinuous canopies. *IEEE Transactions on Geoscience and Remote Sensing* 33, 466-480.
- Reitzel, R., Gillespie, A. R., Weiske, R., and Haugerud, R., 2002. Parsing the Shade Fraction of a TM Image Using Lidar Data, Kitsap County, Washington. American Society of Photogrammetry and Remote Sensing Conference, Seattle, WA, Fall.
- Roberts, D.A., Adams, J.B., and Smith, M.O., 1993. Discriminating green vegetation, non-photosynthetic vegetation and soils in AVIRIS Data. *Remote Sensing of Environment* 44(2/3), 255-270.
- Sabol, D. E., Jr., Gillespie, A. R., Adams, J. B., Smith, M. O., and Tucker, C. J., 2002. Structural stage in Pacific Northwest forests estimated using simple mixing models of multispectral images. *Remote Sensing of Environment* 80(1), 1-16.
- Strahler, A., 1997. Vegetation canopy reflectance modeling - Recent developments and remote sensing perspectives. *Remote Sensing Reviews* 15, 179-194.
- Verhaef, W., 1984. Light scattering by leaf layers with application to canopy reflectance modeling: The SAIL method. *Remote Sensing of Environment* 16, 125-141.

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